

Timothy J. Ross

Fuzzy Logic

With Engineering Applications

Third Edition



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FUZZY LOGIC WITH ENGINEERING APPLICATIONS

Third Edition

FUZZY LOGIC WITH ENGINEERING APPLICATIONS

Third Edition

Timothy J. Ross
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